

# **Nonlinear optical and terahertz spectroscopy of topological semimetals**

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# **Part 1 :band geometry**

- **Introduction to nonlinear optics and a new perspective on band geometry**
- **Discovery of the largest second harmonic generation (SHG) in polar Weyl semimetals TaAs**

# Acknowledgements



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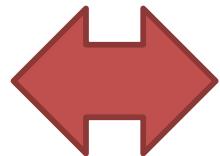
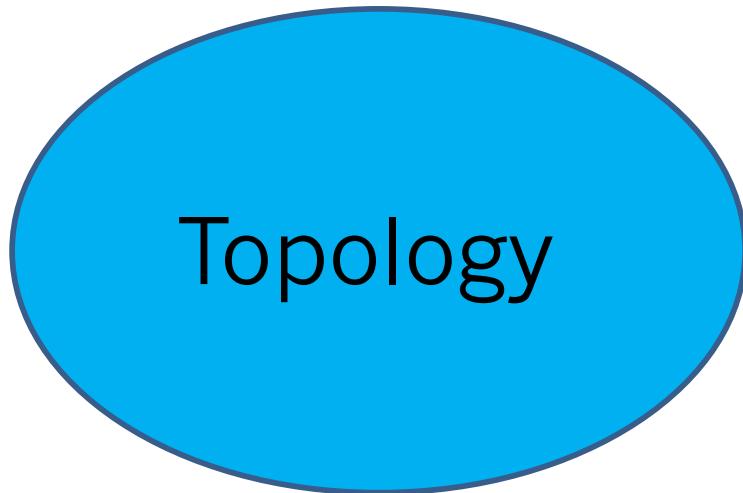
Dan Parker (UCB)

**James Analytis (UCB)**

Nityan Nair (UCB)



# Motivation



- Quantum Hall effect
- Topological insulators
- Weyl semimetal

- Photovoltaics
- Second harmonic generation

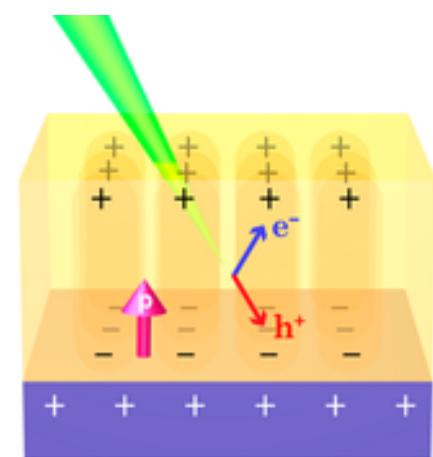
Quantized Hall conductance

(von Klitzing, *PRL*, 80; Chang, Xue. *Science*, 2013)

Quantized Terahertz Faraday & Kerr rotation

(Wu, Armitage. *Science* 2016)

$J_i(0) \propto \sigma^{(2)} I(\omega) \rightarrow$  “bulk photovoltaic effect”



Topological nonlinear optics?

Guidance to find better photovoltaics  
based on topological materials ?

# Part 1

- **Introduction to nonlinear optics and a new perspective on band geometry**
- Discovery of the largest second harmonic generation (SHG) in polar Weyl semimetals TaAs

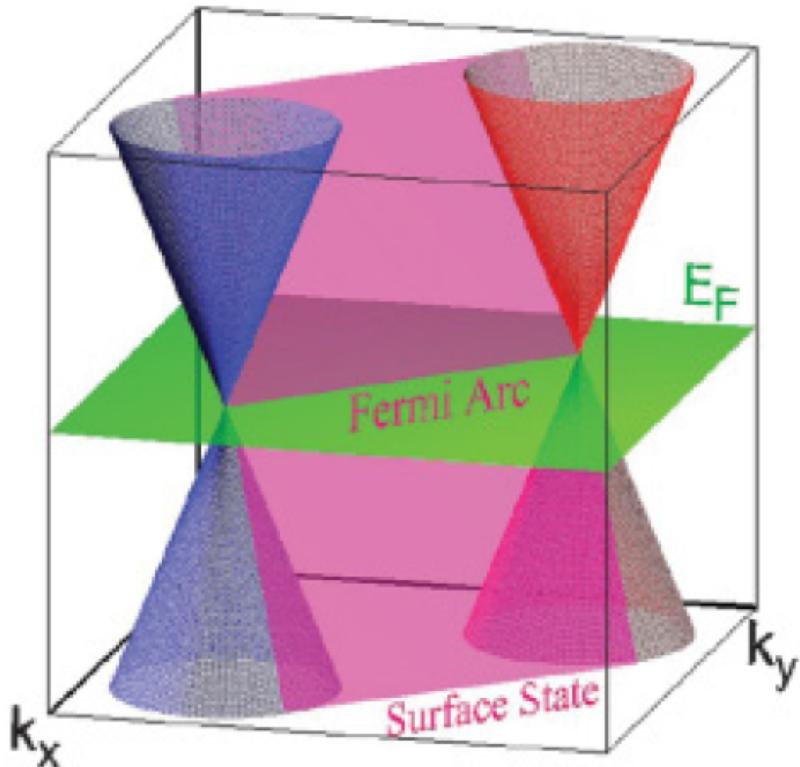
# Weyl semimetals (WSMs)

PHYSICAL REVIEW B **83**, 205101 (2011)



Topological semimetal and Fermi-arc surface states in the electronic structure of pyrochlore iridates

Xiangang Wan,<sup>1</sup> Ari M. Turner,<sup>2</sup> Ashvin Vishwanath,<sup>2,3</sup> and Sergey Y. Savrasov<sup>1,4</sup>



$$H(\mathbf{k}) = \varepsilon_0 \sigma_0 \pm \hbar v_F (\mathbf{k} - \mathbf{k}_0) \cdot \boldsymbol{\sigma}$$

(H. Weyl 1929)

“3D graphene”

Broken Inversion/Time Reversal Symmetry

Murakami. *New. J. Phys.* (2007)  
Wan, et al. *PRB*. (2011)

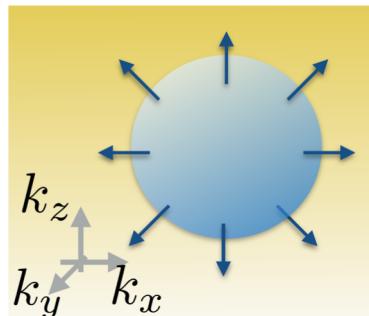
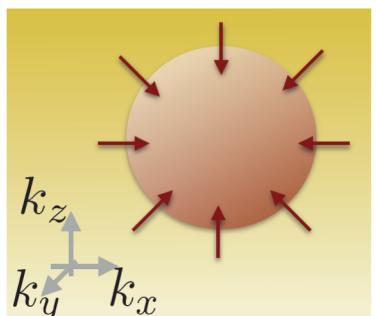
# Band topology in WSMs

Berry curvature

$$\mathbf{A} = -i\langle u_{\mathbf{k}} | \nabla_{\mathbf{k}} u_{\mathbf{k}} \rangle$$

$$\boldsymbol{\Omega}(\mathbf{k}) = \nabla_{\mathbf{k}} \times \mathbf{A}(\mathbf{k})$$

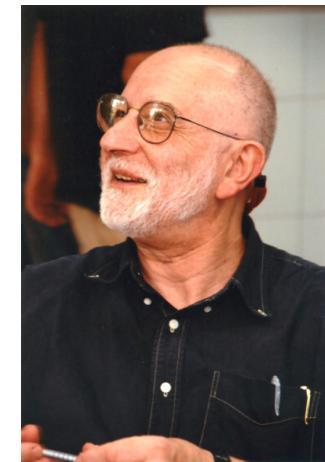
Think of like magnetic field living in k-space  
(Monopoles)



$$\frac{1}{2\pi} \oint_{FS} \boldsymbol{\Omega}(\mathbf{k}) d\mathbf{k} = C_i$$

Berry (geometrical) phase

Sir Michael Berry (1984)



**Nonzero Berry curvature requires breaking of either Inversion or Time-reversal symmetry !**

Inversion symmetry

$$\boldsymbol{\Omega}(\mathbf{k}) = \boldsymbol{\Omega}(-\mathbf{k})$$

Time-reversal symmetry

$$\boldsymbol{\Omega}(\mathbf{k}) = -\boldsymbol{\Omega}(-\mathbf{k})$$

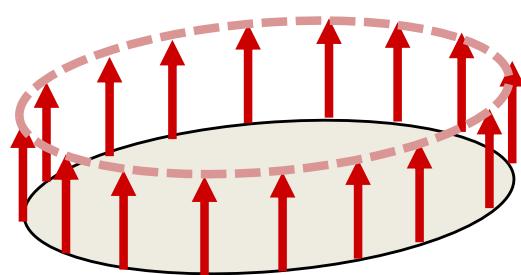
Weyl points are stable unless they meet in momentum space and annihilate each other.

With Both symmetries

$$\boldsymbol{\Omega} = 0$$

# T and I breaking allow new optical phenomena.

Broken T symmetry



$$\langle \Omega(\mathbf{k}) \rangle \neq 0$$

$$\Omega_n(-k) = \Omega_n(k)$$

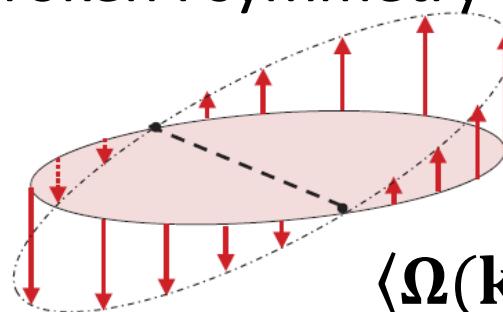
$$j_x = \sigma_{xy} E_y$$

**Intrinsic** Anomalous Hall effect (DC transport)

Faraday and Kerr rotation without applied B

$$\sigma_{xy} = \frac{e^2}{\hbar} \int_{BZ} \frac{d^2 k}{(2\pi)^2} \Omega_{k_x k_y}$$

Broken I symmetry



$$\langle \Omega(\mathbf{k}) \rangle = 0$$

$$\Omega_n(-k) = -\Omega_n(k)$$

$$J_i = \sigma_{ijk} E_j E_k$$

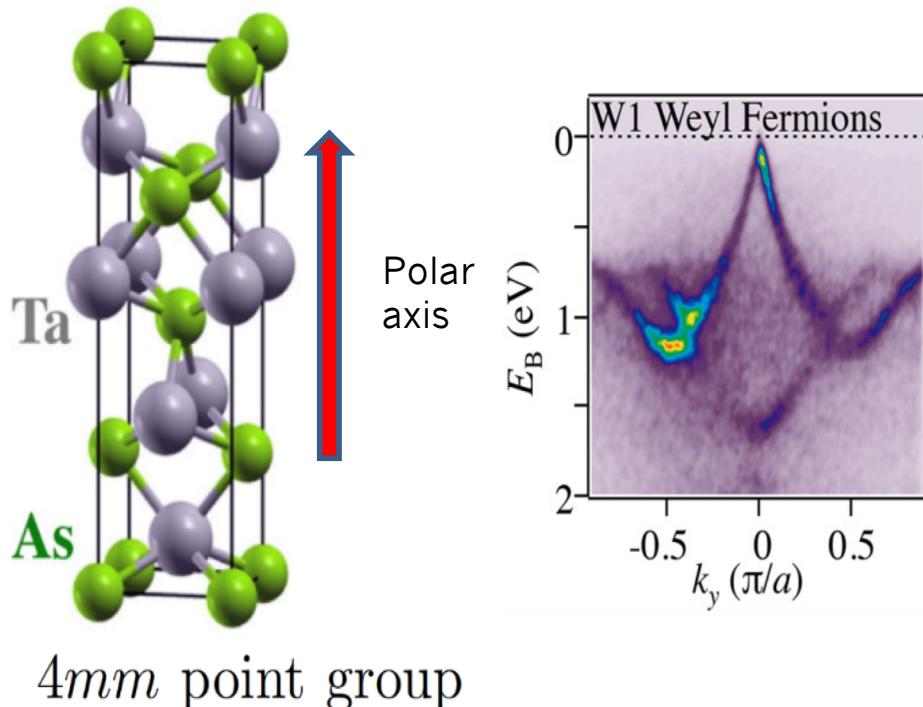
Second order nonlinearity

Zoo of acronymic effects!

**SHG**, DFG, **CPGE**, LPGE, etc.

# Material realization---Transition metal monopnictides

WSMs TaAs, TaP, NbAs, NbP break inversion and are **polar metals** (or ferroelectric metals) !



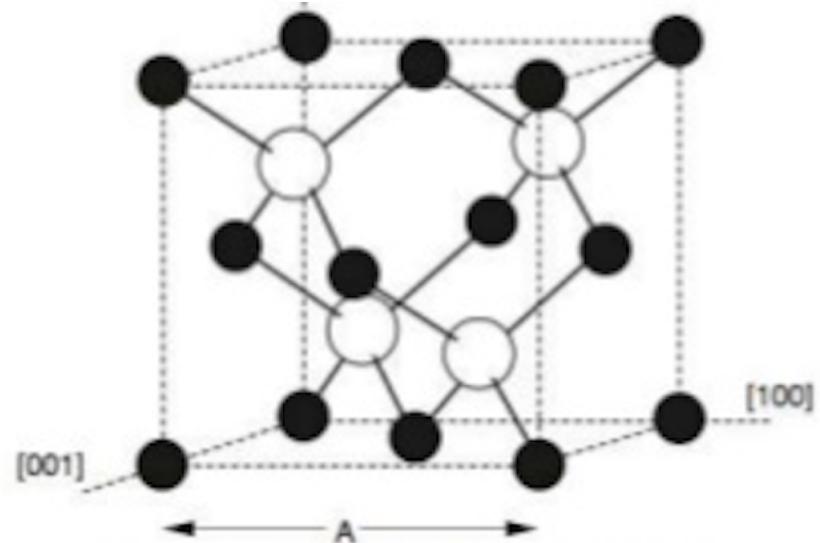
$4mm$  point group

Weng *et al.*, **PRX** (2015)

Huang, *et al.*, **Nat. Comm.** (2015)

Xu, *et al.*, **Science** (2015)

Lv, *et al.*, **PRX** (2015)

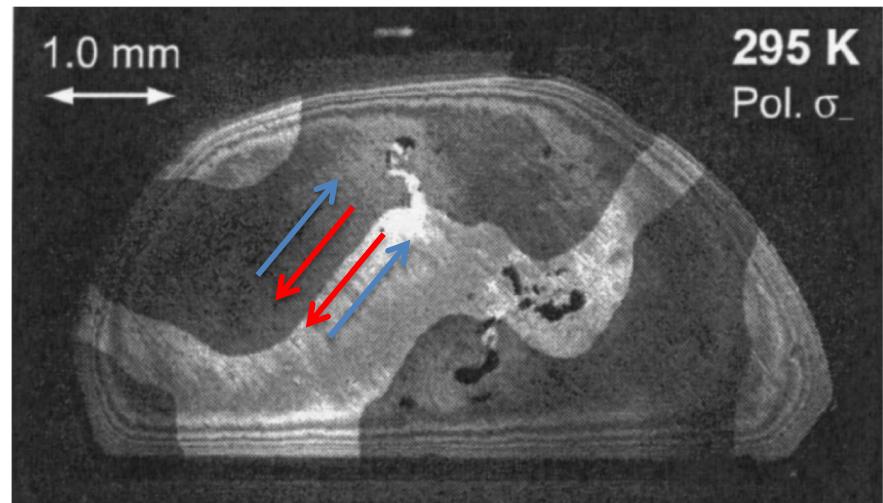
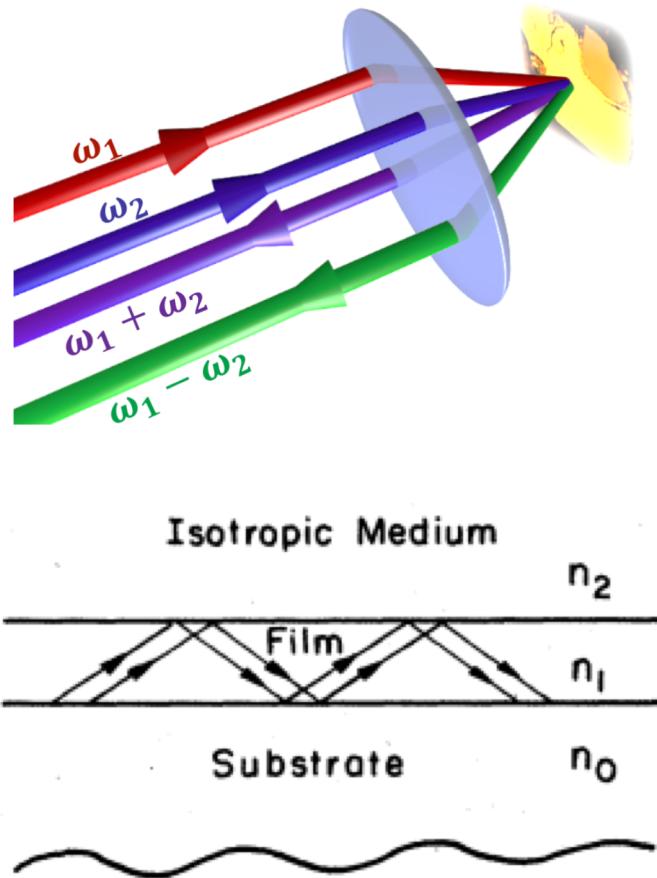


GaAs breaks inversion, but is not polar.

**Are there new/enhanced transport and optics  
effects in inversion-breaking WSMs  
associated Berry monopoles?**

# Past nonlinear optics

Focused on probing light conversion and symmetry breaking.



$\text{Cr}_2\text{O}_3$

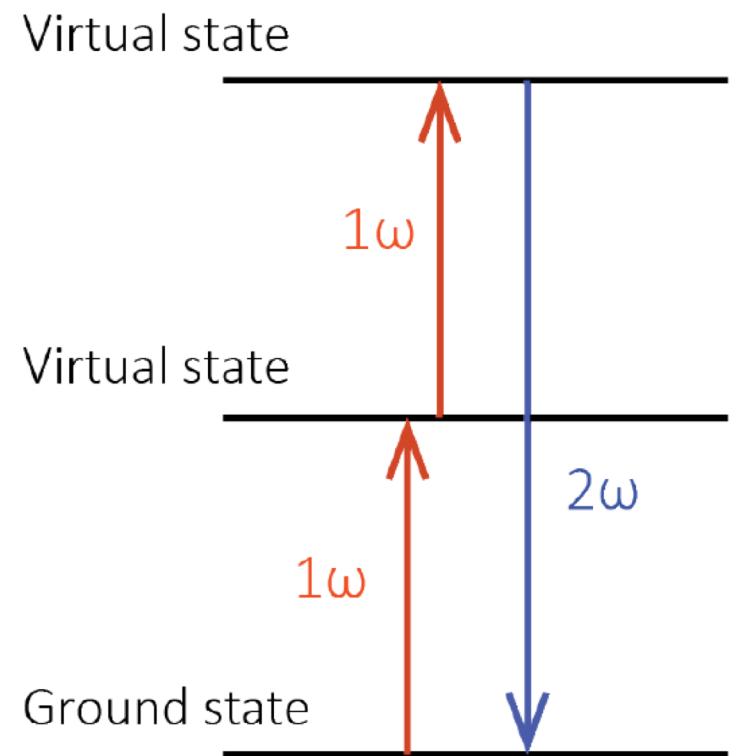
Fiebig, et al. *JOSA* (2005)

Y. R. Shen, *RMP* (1976)

# Why nonlinear optics experiments on WSMs?

*How textbooks calculate nonlinear optical susceptibility....*

$$\begin{aligned}
 & \chi_{\mu\alpha\beta}^{(2)}(-2\omega, \omega, \omega) \\
 &= -i \frac{1}{32\epsilon_0} \left( \frac{e}{m_0 \pi \omega} \right)^3 \sum_{n,n',n''} \int_{\text{BZ}} d^3 \mathbf{k} \\
 & \times f_{n\mathbf{k}} \left\{ \frac{p_{nn'}^\mu p_{n'n''}^\alpha p_{n''n}^\beta + p_{nn'}^\mu p_{n'n''}^\beta p_{n''n}^\alpha}{[E_{n'n}(\mathbf{k}) - 2\hbar\omega][E_{n''n}(\mathbf{k}) - \hbar\omega]} \right. \\
 & + \frac{p_{nn'}^\alpha p_{n'n''}^\mu p_{n''n}^\beta + p_{nn'}^\beta p_{n'n''}^\mu p_{n''n}^\alpha}{[E_{n'n}(\mathbf{k}) + \hbar\omega][E_{n''n}(\mathbf{k}) - \hbar\omega]} \\
 & \left. + \frac{p_{nn'}^\beta p_{n'n''}^\alpha p_{n''n}^\mu + p_{nn'}^\alpha p_{n'n''}^\beta p_{n''n}^\mu}{[E_{n'n}(\mathbf{k}) + \hbar\omega][E_{n''n}(\mathbf{k}) + 2\hbar\omega]} \right\}, \\
 & \mu, \alpha, \beta \in \{x, y, z\}.
 \end{aligned}$$



# Why nonlinear optics experiments on WSMs?

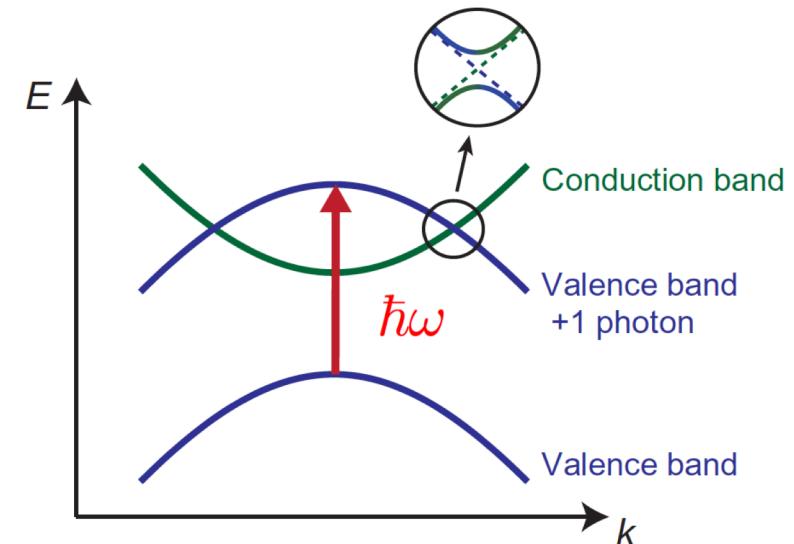
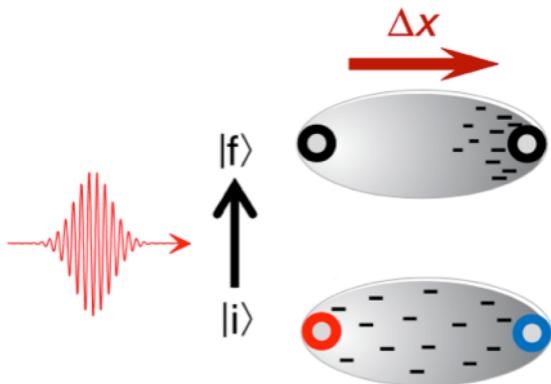
## --- Probing Berry Connection & band topology

$$a_n(\mathbf{k}) = -i\langle u_{nk} | \nabla_{\mathbf{k}} u_{nk} \rangle$$

$$\varphi_{12} = \text{Im}(\log v_{12}^0)$$

$$R_k = \left[ \frac{\partial \varphi_{12}}{\partial k} + a_1 - a_2 \right]$$

**"Shift vector"** measures the change of intracell coordinates in the transition between the initial and final states.



Von Baltz **PRB** (1979) (1981); Sturman & Fridkin & Belinicher **SPU** (1980) (1992); Sipe & Shkrebta **PRB**. (2000); Young & Rappe **PRL** 2012; Morimoto & Nagaosa **Sci. Adv.** (2016)

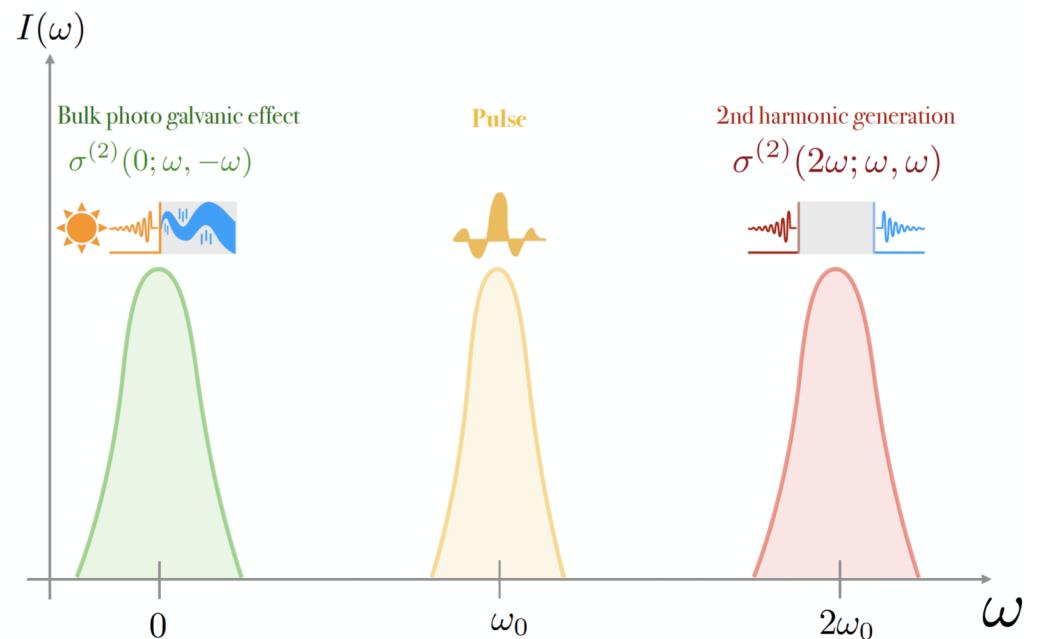
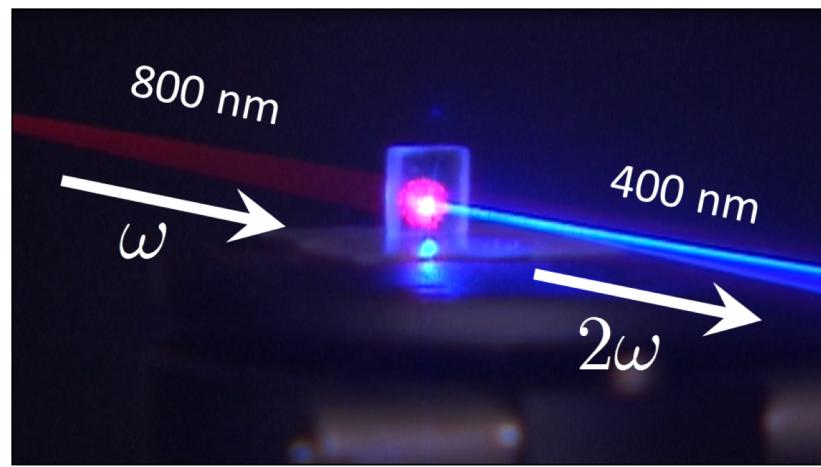
$$\text{Re}\{\sigma_{zzz}^{(2)}(\omega, 0)\} \cong \frac{\pi e^3}{2\hbar\omega^2} \int \frac{d^3\mathbf{k}}{(2\pi)^3} |v_{z,12}|^2 R_{zz}(\mathbf{k})$$

$$\times \left[ -\delta(\epsilon_{21} - \hbar\omega) + \right]$$

# 2<sup>nd</sup> order nonlinear optical effect in general

$$J_i(\omega_1 \pm \omega_2) = \sigma_{ijk}(\omega_1 \pm \omega_2) E_j(\omega_1) E_k(\omega_2)$$

sum and difference frequency generation



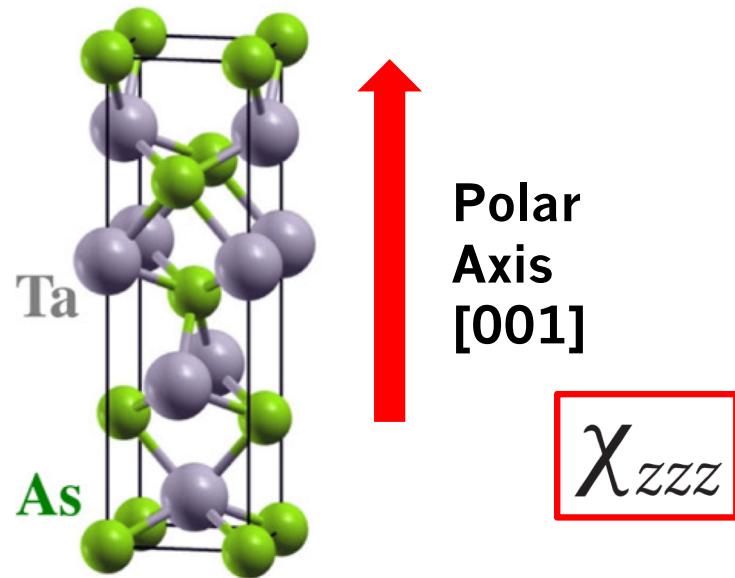
# Second harmonic generation (SHG)

In materials without inversion symmetry,

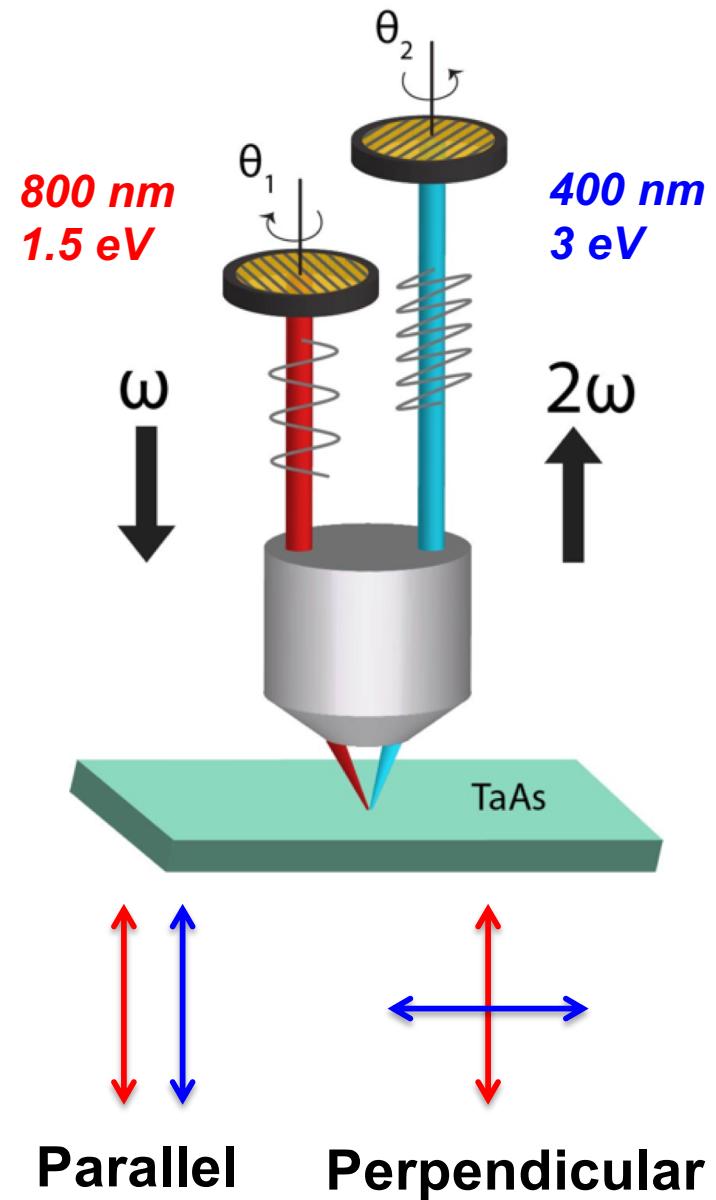
$$\mathbf{P} = \mathbf{P}_0 + \epsilon_0 \chi_e \mathbf{E} + \epsilon_0 \chi^{(2)} \mathbf{E}^2 + \dots$$

$$P_i(2\omega) = \epsilon_0 \chi_{ijk}(2\omega) E_j(\omega) E_k(\omega)$$

Bloembergen & Pershan. *Phys. Rev* (1962)



Mirror plane  $xz$  &  $yz$ , but not  $xy$

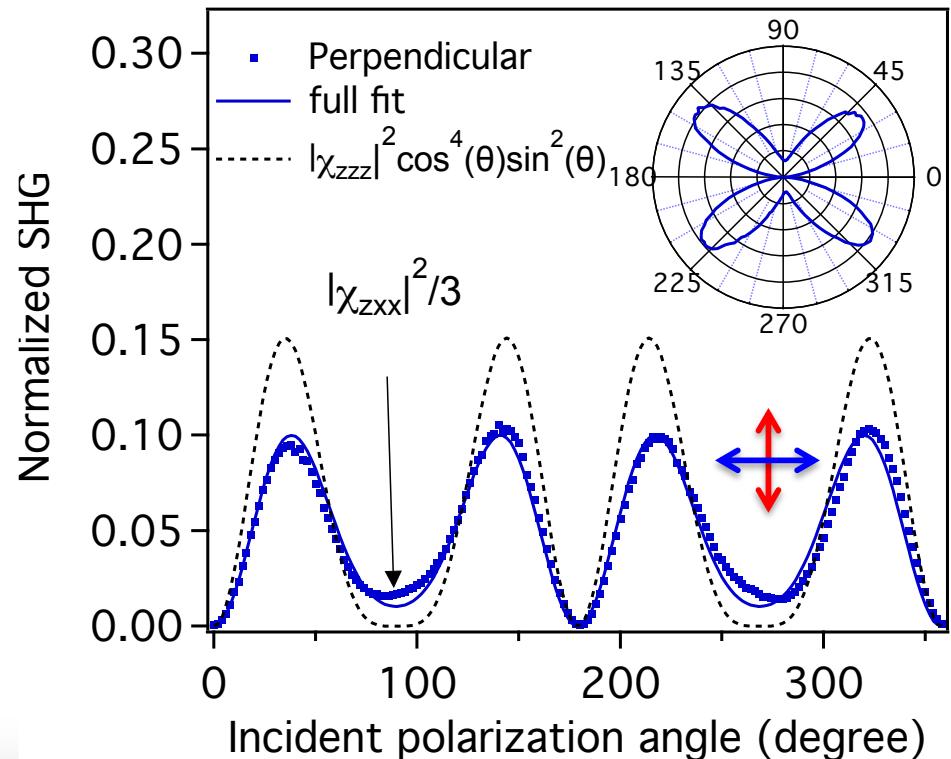
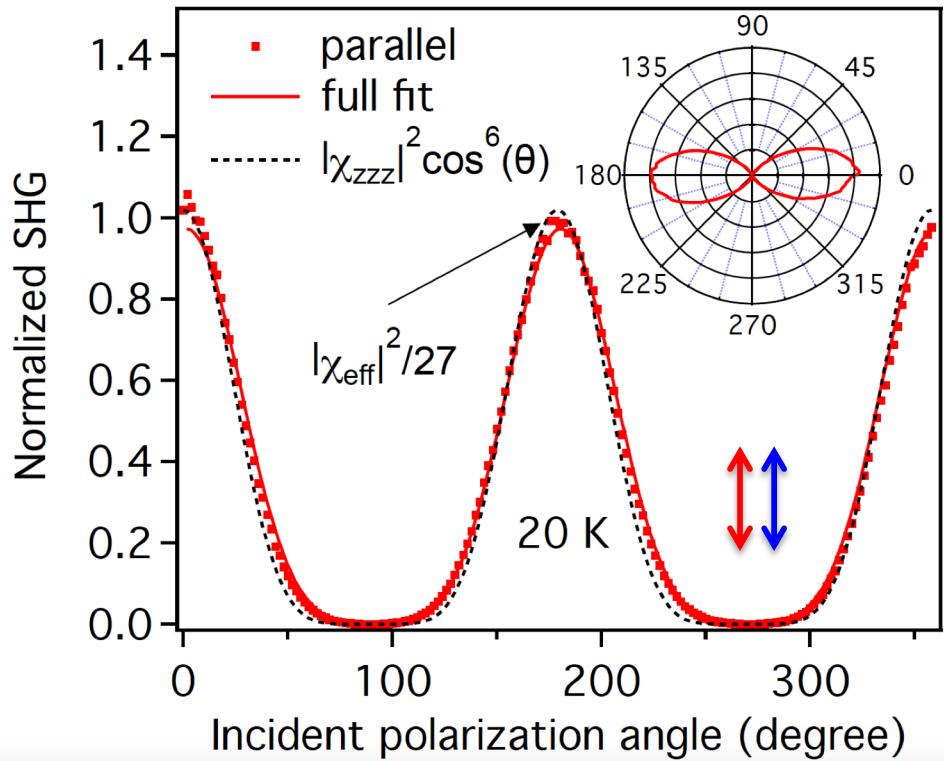


4mm point group determines **three** non-zero  $\chi_{ijk}$ .

# Part 1

- Introduction to nonlinear optics and a new perspective on band geometry
- **Discovery of the largest second harmonic generation (SHG) in polar Weyl semimetals TaAs**

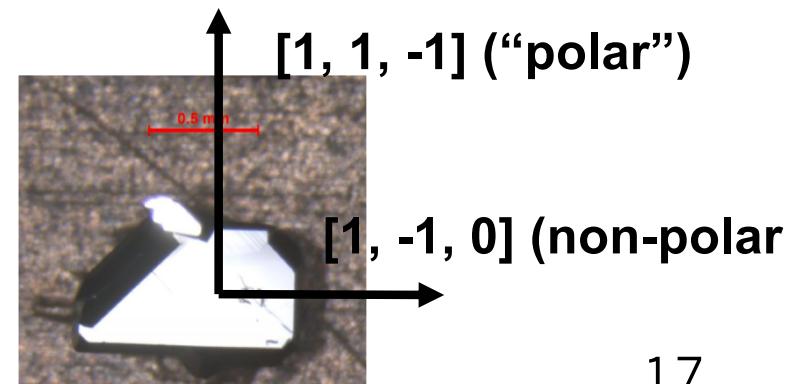
# SHG on TaAs (112) surface



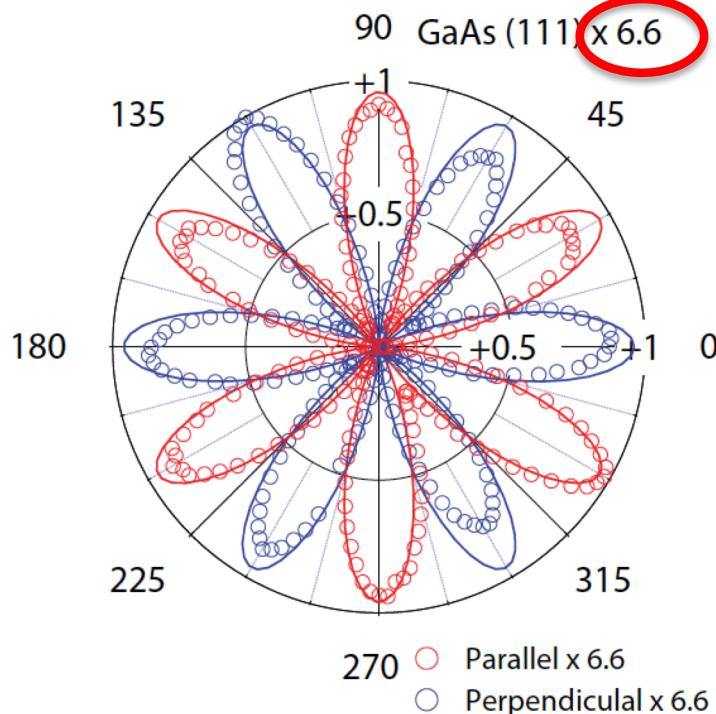
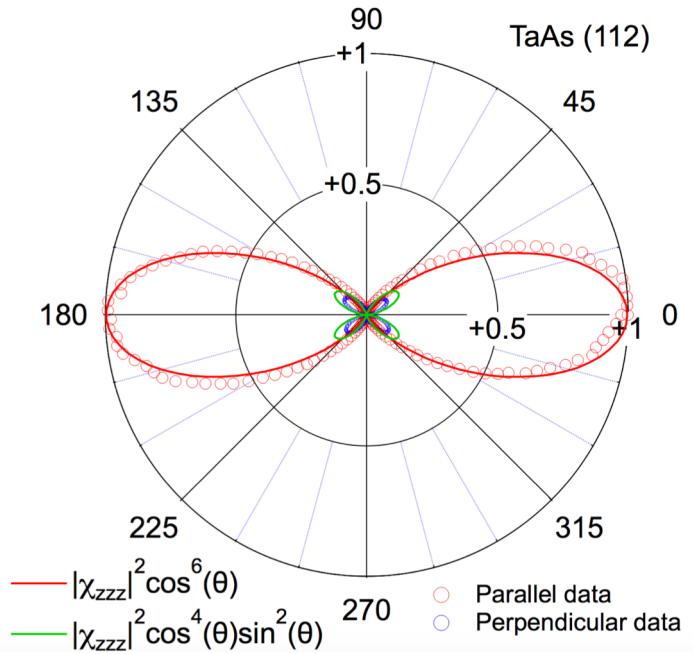
Dominating  $\chi_{\text{zzz}}$ . ( effectively 1D-like )

Anisotropy  $\chi_{\text{zzz}}/\chi_{\text{zxx}}, \chi_{\text{zzz}}/\chi_{\text{xzx}}$  30-100 in TaAs !  
 Materials with same  $\chi_{ijk}$  tensor have anisotropy factor 1-2. e.g. LiNbO<sub>3</sub>, BaTiO<sub>3</sub>

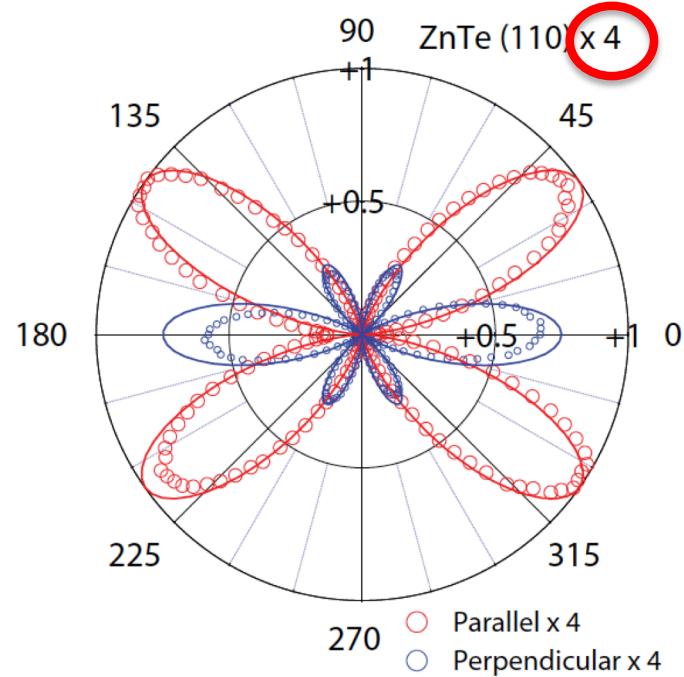
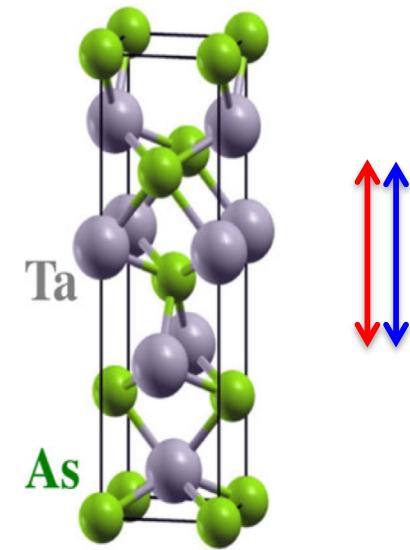
Wu, et al. [arXiv:1609.04894](https://arxiv.org/abs/1609.04894)  
*Nat. Phys.* (2016)



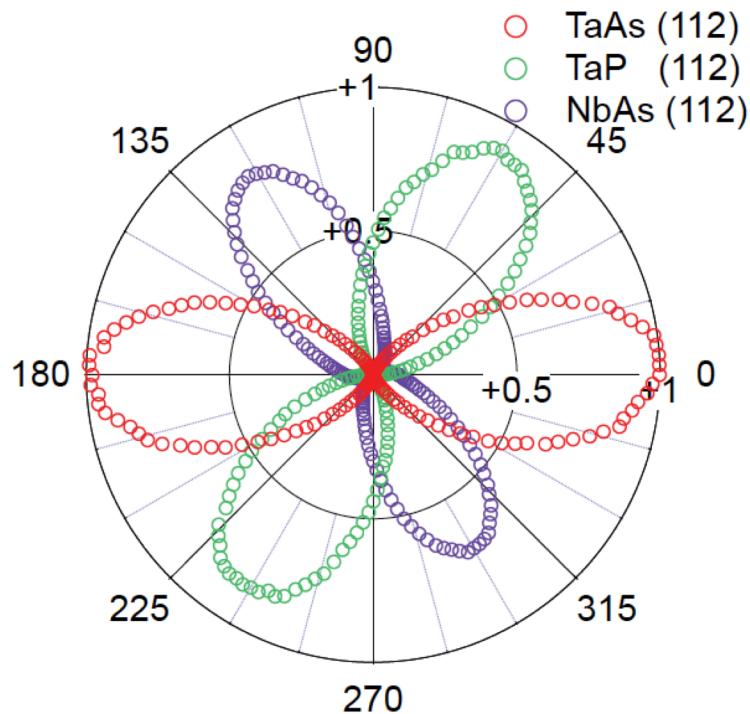
# Largest SHG in existing materials



TaAs (100) will  
have SHG  
intensity **>100**  
times bigger  
than GaAs  
(111)!



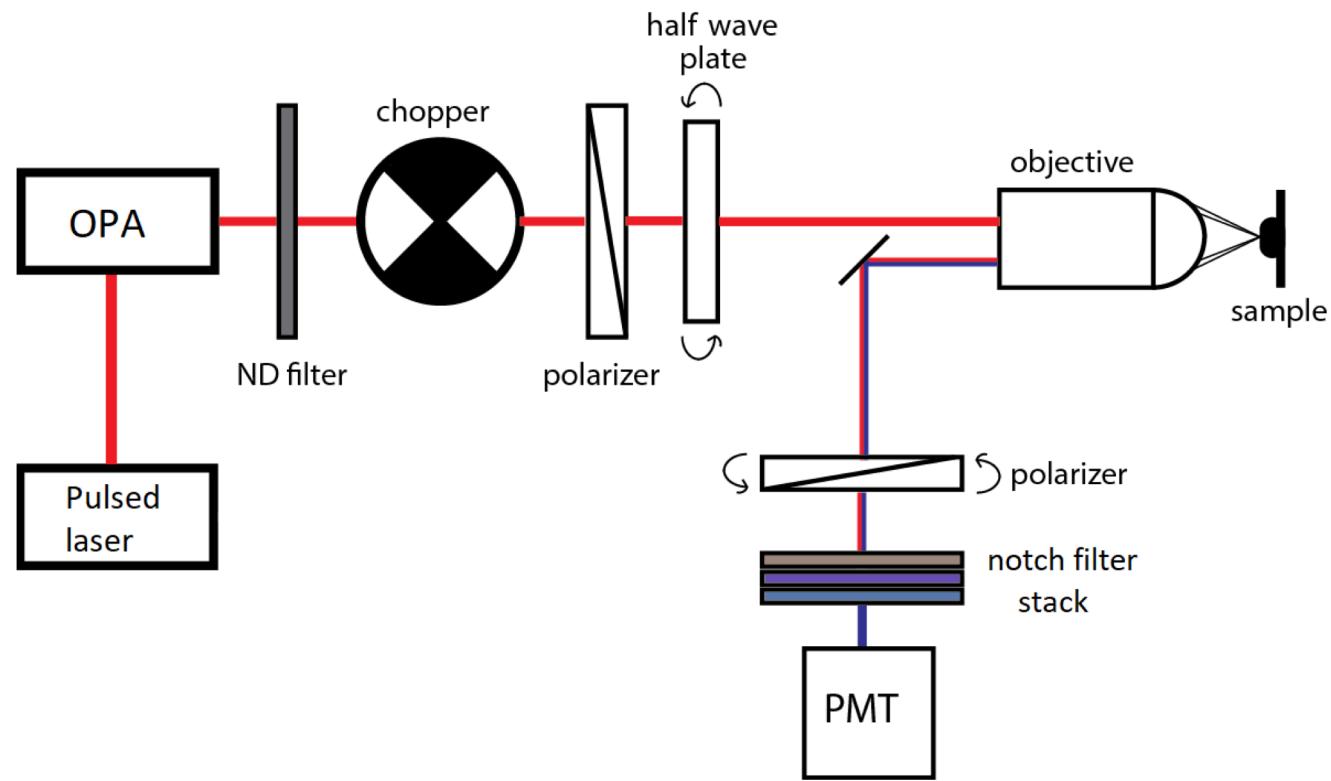
# Other WSMs TaP & NbAs



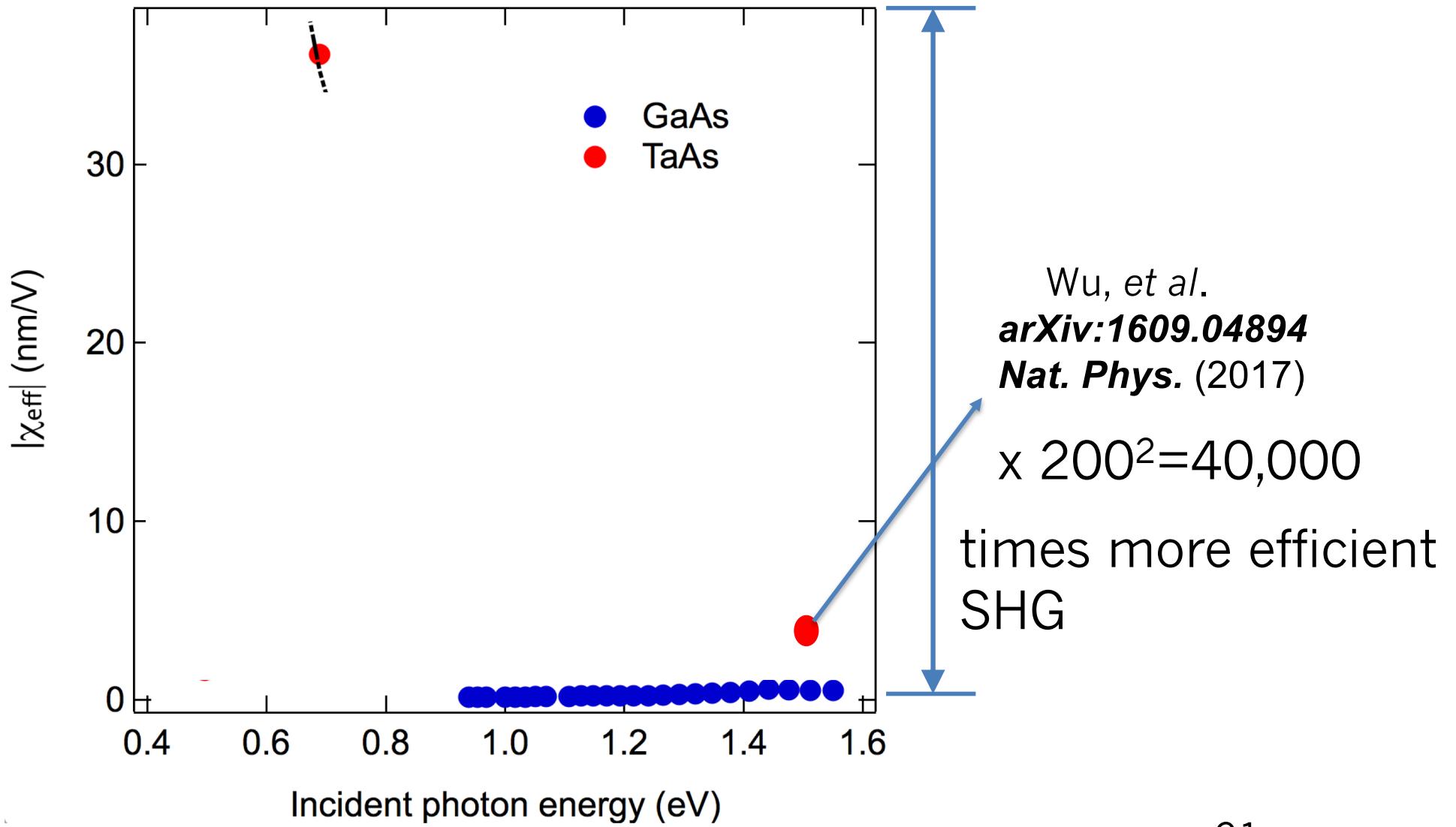
Material	$ \chi_{ijk} $	$ \chi $ (pm/V)	Fundamental wavelength (nm)
TaAs	$\chi_{zzz}$	7200 ( $\pm 1100$ )	800
GaAs	$\chi_{xyz}$	700*	810
ZnTe	$\chi_{xyz}$	500, 900*	800, 700
BaTiO <sub>3</sub>	$\chi_{zzz}$	30	900
BiFeO <sub>3</sub>	$\chi_{zzz}$	30-40	1550, 800
LiNbO <sub>3</sub>	$\chi_{zzz}$	50	852
BiFeO <sub>3</sub>	$\chi_{zzz}$	260*	500
BaTiO <sub>3</sub>	$\chi_{zzz}$	200*	170
PbTiO <sub>3</sub>	$\chi_{zzz}$	400*	150

Wu, et al. *arXiv:1609.04894*  
*Nat. Phys.* 13, 350(2017)

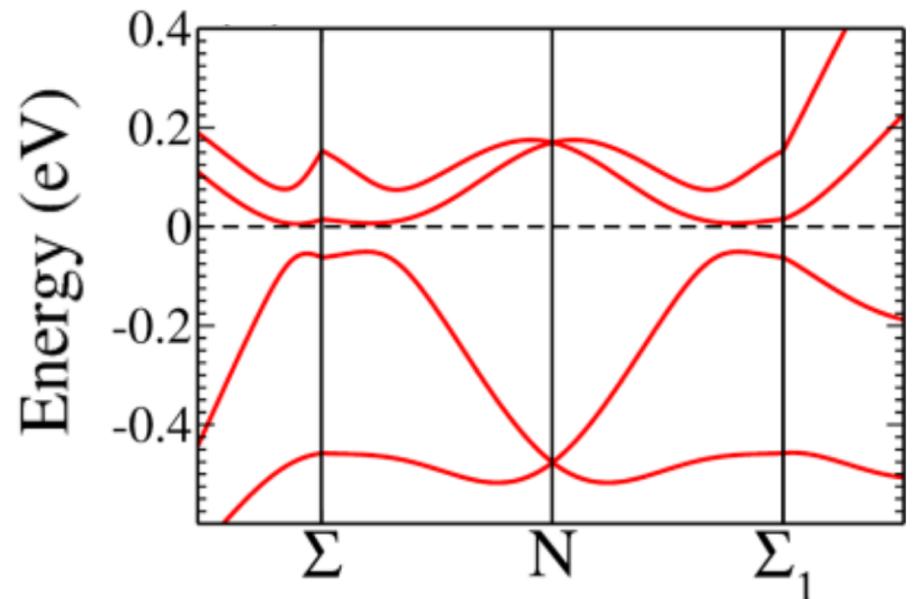
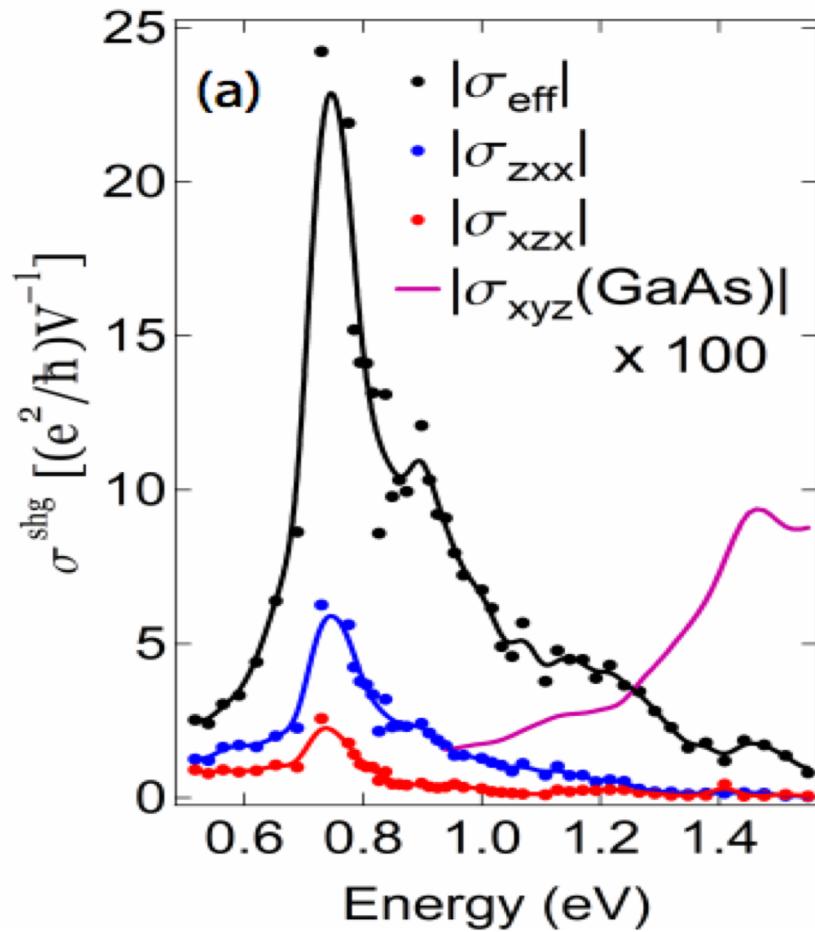
# Spectroscopy of SHG response in range 0.4 eV – 1.6 eV



# For fundamental and SH electric field along polar axis

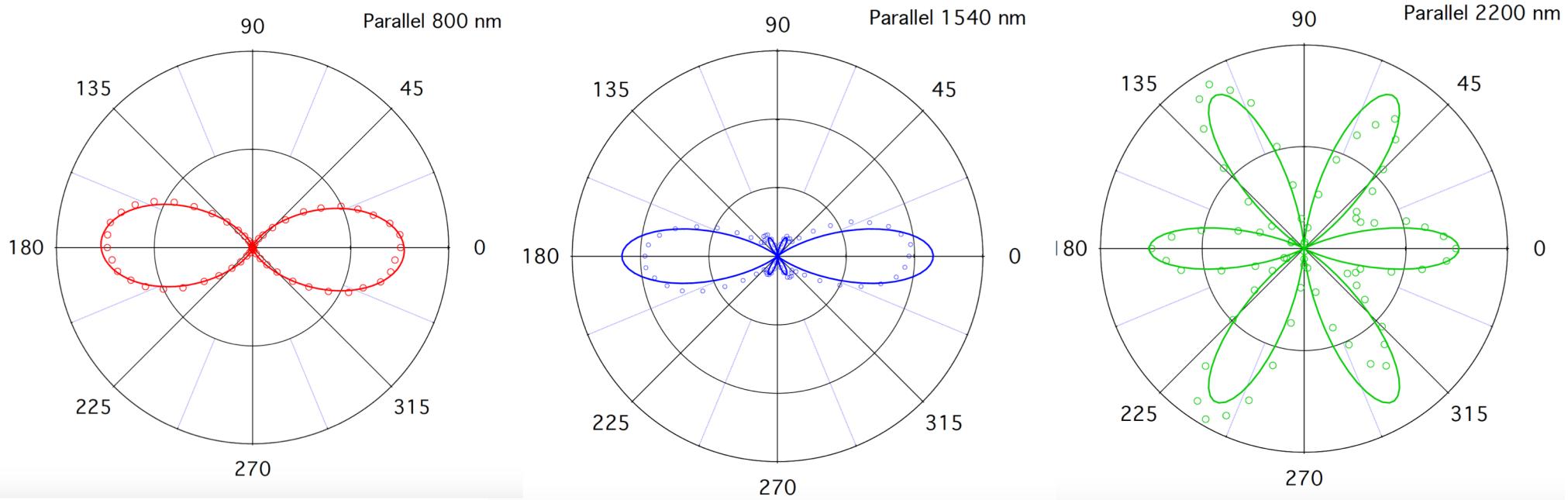


# Resonance enhanced peak

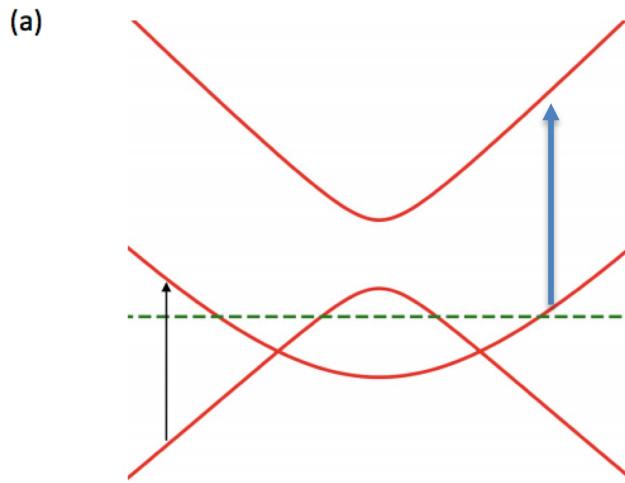


Weng et al., *PRX* (2015)  
Huang, et al., *Nat. Comm.* (2015)  
J. Buckeridge et al. *PRB*, (2016)

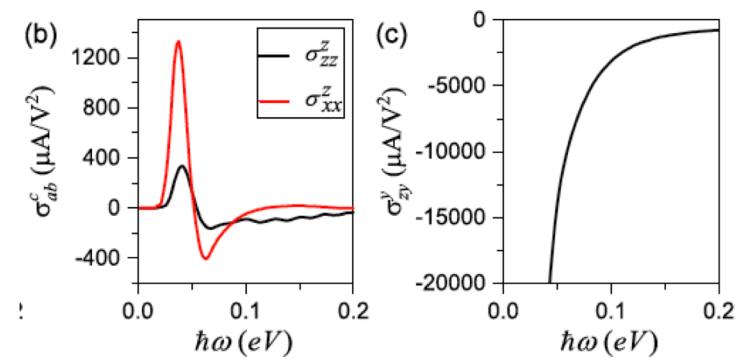
# Change of polar pattern



# Is Weyl physics related?

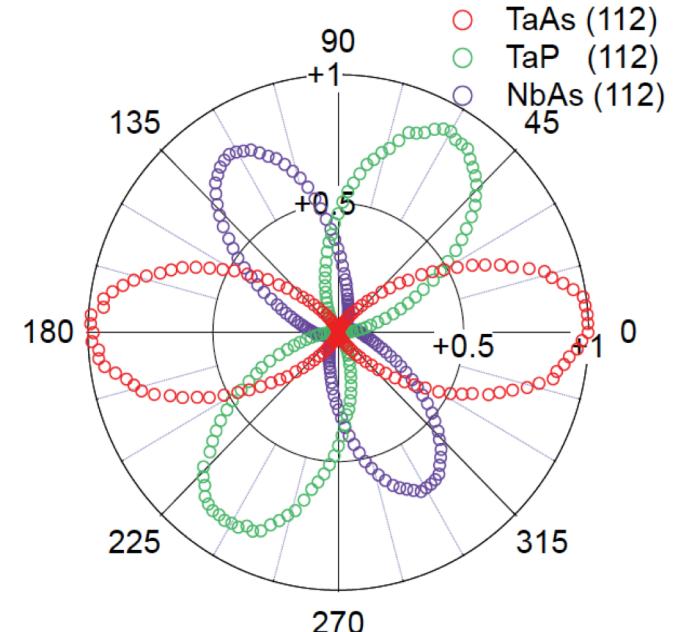


In addition, the calculated SH susceptibility  $\chi_{zz}^z$  and the ratio of  $\chi_{zx}^x/\chi_{zz}^z$  are 6200 pm/V and 0.3 respectively, which are quite closed to the measured value 7200 pm/V and 0.031 at low temperature [45, 59].

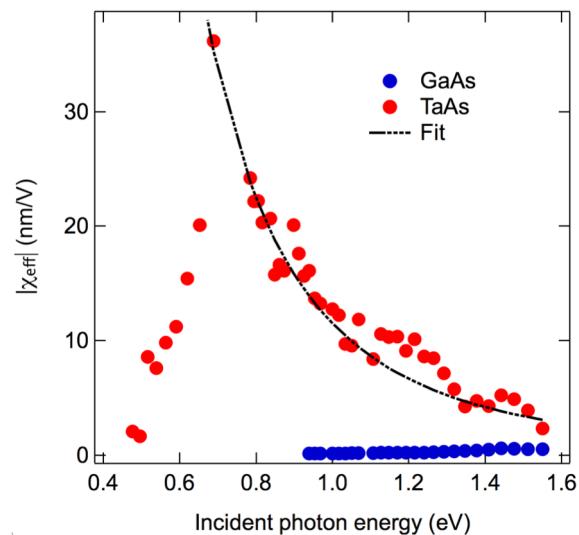


# Summary

- Discovery of the largest SHG in WSMs TaAs, TaP and NbAs
- A new perspective nonlinear optics in probing Berry connection/curvature



Wu, et al. *arXiv:1609.04894*  
*Nat. Phys.* 13, 350 (2017)



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*arXiv:1804.06973, PRB (2018)*



Thanks !

